Sikshapath

Q1) Find the curve of second degree of regression of y on x () to the following data by method of least square :

| X | 1 | 2 | 3 | 4 |
|---|---|----|----|----|
| y | 6 | 11 | 18 | 27 |

Sol:

| х | 1 | 2 | 3 | 4 | |
|---|---|----|----|----|--|
| y | 6 | 11 | 18 | 27 | |

Sol. We form the following table:

| x | у | x^2 | x^3 | x ⁴ | ху | x^2y |
|-----------------|-----------------|-------------------|--------------------|--------------------|-------------------|----------------------|
| 1 | 6 | 1 | 1 | 1 | 6 | 6 |
| 2 | 11 | 4 | 8 | 16 | 22 | 44 |
| 3 | 18 | 9 | 27 | 81 | 54 | 162 |
| 4 | 27 | 16 | 64 | 256 | 108 | 432 |
| $\Sigma x = 10$ | $\Sigma y = 62$ | $\Sigma x^2 = 30$ | $\Sigma x^3 = 100$ | $\Sigma x^4 = 354$ | $\Sigma xy = 190$ | $\Sigma x^2 y = 644$ |

The equation of second degree parabola is given by

$$y = a + bx + cx^2 \qquad \dots (1)$$

And the normal equations are

$$\Sigma y = an + b\Sigma x + c\Sigma x^2 \qquad ...(2)$$

$$\sum xy = a\sum x + b\sum x^2 + c\sum x^3 \qquad ...(3)$$

$$\sum x^2 y = a \sum x^2 + b \sum x^3 + c \sum x^4 \qquad \dots (4)$$

$$\Rightarrow 4a + 10b + 30c = 62
10a + 30b + 100c = 190
30a + 100b + 354c = 644
\Rightarrow a = 3, b = 2, c = 1$$

Hence $y = 3 + 2x + x^2$. **Ans.**